

Markscheme

May 2024

Mathematics: analysis and approaches

Standard level

Paper 2

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Instructions to Examiners

Abbreviations

- M** Marks awarded for attempting to use a correct **Method**.
- A** Marks awarded for an **Answer** or for **Accuracy**; often dependent on preceding **M** marks.
- R** Marks awarded for clear **Reasoning**.
- AG** Answer given in the question and so no marks are awarded.
- FT** Follow through. The practice of awarding marks, despite candidate errors in previous parts, for their correct methods/answers using incorrect results.

Using the markscheme

1 General

Award marks using the annotations as noted in the markscheme *eg M1, A2*.

2 Method and Answer/Accuracy marks

- Do **not** automatically award full marks for a correct answer; all working **must** be checked, and marks awarded according to the markscheme.
- It is generally not possible to award **M0** followed by **A1**, as **A** mark(s) depend on the preceding **M** mark(s), if any.
- Where **M** and **A** marks are noted on the same line, *e.g. M1A1*, this usually means **M1** for an **attempt** to use an appropriate method (*e.g.* substitution into a formula) and **A1** for using the **correct** values.
- Where there are two or more **A** marks on the same line, they may be awarded independently; so if the first value is incorrect, but the next two are correct, award **A0A1A1**.
- Where the markscheme specifies **A3**, **M2** *etc.*, do **not** split the marks, unless there is a note.
- The response to a “show that” question does not need to restate the **AG** line, unless a **Note** makes this explicit in the markscheme.
- Once a correct answer to a question or part question is seen, ignore further working even if this working is incorrect and/or suggests a misunderstanding of the question. This will encourage a uniform approach to marking, with less examiner discretion. Although some candidates may be advantaged for that specific question item, it is likely that these candidates will lose marks elsewhere too.
- An exception to the previous rule is when an incorrect answer from further working is used **in a subsequent part**. For example, when a correct exact value is followed by an incorrect decimal approximation in the first part and this approximation is then used in the second part. In this situation, award **FT** marks as appropriate but do not award the final **A1** in the first part.

Examples:

	Correct answer seen	Further working seen	Any FT issues?	Action
1.	$8\sqrt{2}$	5.65685... (incorrect decimal value)	No. Last part in question.	Award A1 for the final mark (condone the incorrect further working)
2.	$\frac{35}{72}$	0.468111... (incorrect decimal value)	Yes. Value is used in subsequent parts.	Award A0 for the final mark (and full FT is available in subsequent parts)

3 Implied marks

Implied marks appear in **brackets e.g. (M1)**, and can only be awarded if **correct** work is seen or implied by subsequent working/answer.

4 Follow through marks (only applied after an error is made)

Follow through (**FT**) marks are awarded where an incorrect answer from one **part** of a question is used correctly in **subsequent** part(s) (e.g. incorrect value from part (a) used in part (d) or incorrect value from part (c)(i) used in part (c)(ii)). Usually, to award **FT** marks, **there must be working present** and not just a final answer based on an incorrect answer to a previous part. However, if all the marks awarded in a subsequent part are for the answer or are implied, then **FT** marks should be awarded for *their* correct answer, even when working is not present.

For example: following an incorrect answer to part (a) that is used in subsequent parts, where the markscheme for the subsequent part is **(M1)A1**, it is possible to award full marks for *their* correct answer, **without working being seen**. For longer questions where all but the answer marks are implied this rule applies but may be overwritten by a **Note** in the Markscheme.

- Within a question part, once an **error** is made, no further **A** marks can be awarded for work which uses the error, but **M** marks may be awarded if appropriate.
- If the question becomes much simpler because of an error then use discretion to award fewer **FT** marks, by reflecting on what each mark is for and how that maps to the simplified version.
- If the error leads to an inappropriate value (e.g. probability greater than 1, $\sin \theta = 1.5$, non-integer value where integer required), do not award the mark(s) for the final answer(s).
- The markscheme may use the word “their” in a description, to indicate that candidates may be using an incorrect value.
- If the candidate’s answer to the initial question clearly contradicts information given in the question, it is not appropriate to award any **FT** marks in the subsequent parts. This

includes when candidates fail to complete a “show that” question correctly, and then in subsequent parts use their incorrect answer rather than the given value.

- Exceptions to these **FT** rules will be explicitly noted on the markscheme.
- If a candidate makes an error in one part but gets the correct answer(s) to subsequent part(s), award marks as appropriate, unless the command term was “Hence”.

5 Mis-read

If a candidate incorrectly copies values or information from the question, this is a mis-read (**MR**). A candidate should be penalized only once for a particular misread. Use the **MR** stamp to indicate that this has been a misread and do not award the first mark, even if this is an **M** mark, but award all others as appropriate.

- If the question becomes much simpler because of the **MR**, then use discretion to award fewer marks.
- If the **MR** leads to an inappropriate value (e.g. probability greater than 1, $\sin \theta = 1.5$, non-integer value where integer required), do not award the mark(s) for the final answer(s).
- Miscopying of candidates’ own work does **not** constitute a misread, it is an error.
- If a candidate uses a correct answer, to a “show that” question, to a higher degree of accuracy than given in the question, this is NOT a misread and full marks may be scored in the subsequent part.
- **MR** can only be applied when work is seen. For calculator questions with no working and incorrect answers, examiners should **not** infer that values were read incorrectly.

6 Alternative methods

Candidates will sometimes use methods other than those in the markscheme. Unless the question specifies a method, other correct methods should be marked in line with the markscheme. If the command term is ‘Hence’ and not ‘Hence or otherwise’ then alternative methods are not permitted unless covered by a note in the mark scheme.

- Alternative methods for complete questions are indicated by **METHOD 1**, **METHOD 2**, etc.
- Alternative solutions for parts of questions are indicated by **EITHER . . . OR**.

7 Alternative forms

Unless the question specifies otherwise, **accept** equivalent forms.

- As this is an international examination, accept all alternative forms of **notation** for example 1.9 and 1,9 or 1000 and 1,000 and 1.000.
- Do not accept final answers written using calculator notation. However, **M** marks and intermediate **A** marks can be scored, when presented using calculator notation, provided the evidence clearly reflects the demand of the mark.
- In the markscheme, equivalent **numerical** and **algebraic** forms will generally be written in brackets immediately following the answer.
- In the markscheme, some **equivalent** answers will generally appear in brackets. Not all equivalent notations/answers/methods will be presented in the markscheme and examiners are asked to apply appropriate discretion to judge if the candidate work is equivalent.

8 Format and accuracy of answers

If the level of accuracy is specified in the question, a mark will be linked to giving the answer to the required accuracy. If the level of accuracy is not stated in the question, the general rule applies to final answers: *unless otherwise stated in the question all numerical answers must be given exactly or correct to three significant figures*.

Where values are used in subsequent parts, the markscheme will generally use the exact value, however candidates may also use the correct answer to 3 sf in subsequent parts. The markscheme will often explicitly include the subsequent values that come “*from the use of 3 sf values*”.

Simplification of final answers: Candidates are advised to give final answers using good mathematical form. In general, for an **A** mark to be awarded, arithmetic should be completed,

and any values that lead to integers should be simplified; for example, $\sqrt{\frac{25}{4}}$ should be written

as $\frac{5}{2}$. An exception to this is simplifying fractions, where lowest form is not required (although

the numerator and the denominator must be integers); for example, $\frac{10}{4}$ may be left in this form

or written as $\frac{5}{2}$. However, $\frac{10}{5}$ should be written as 2, as it simplifies to an integer.

Algebraic expressions should be simplified by completing any operations such as addition and multiplication, e.g. $4e^{2x} \times e^{3x}$ should be simplified to $4e^{5x}$, and $4e^{2x} \times e^{3x} - e^{4x} \times e^x$ should be simplified to $3e^{5x}$. Unless specified in the question, expressions do not need to be factorized, nor do factorized expressions need to be expanded, so $x(x+1)$ and $x^2 + x$ are both acceptable.

Please note: intermediate **A** marks do NOT need to be simplified.

9 Calculators

A GDC is required for this paper, but if you see work that suggests a candidate has used any calculator not approved for IB DP examinations (eg CAS enabled devices), please follow the procedures for malpractice.

10. Presentation of candidate work

Crossed out work: If a candidate has drawn a line through work on their examination script, or in some other way crossed out their work, do not award any marks for that work unless an explicit note from the candidate indicates that they would like the work to be marked.

More than one solution: Where a candidate offers two or more different answers to the same question, an examiner should only mark the first response unless the candidate indicates otherwise. If the layout of the responses makes it difficult to judge, examiners should apply appropriate discretion to judge which is “first”.

Section A

1. (a) median = 75 **A1**
 (upper quartile =) 84 OR (lower quartile =) 68 **(A1)**
 Interquartile range = 16 **A1**
[3 marks]

(b)

Note: In this part, their reasoning and answer must be consistent with their values in part (a).

In both part (i) and part (ii), award **R0A1** for a correct answer with no reasoning.

- (i) $80 > 75$ OR Australia has a higher median OR Spain's median is lower **R1**

Note: Award **R1** for correct reasoning based on a comparison of their medians.

in general (on average), rabbits in Australia have longer ears (than rabbits in Spain)

OR

in the top 50% of each distribution, some rabbits in Spain have smaller ears than those in Australia

OR

in the bottom 50% of each distribution, some rabbits in Australia have longer ears than those in Spain **A1**

- (ii) $16 > 11$ OR higher IQR in Spain OR lower IQR in Australia **R1**

Note: Award **R1** for correct reasoning based on a comparison of their IQR's.

(the IQR's suggest that) there is more variation/spread in (the middle 50% of) rabbit ears in Spain (than those in Australia) (or equivalent) **A1**

Note: Award **A1** for any correct answer which uses the IQR's to compare each distribution.

[4 marks]

Total [7 marks]

2. (a) recognition that a 15% loss leaves 85% OR finding 15% and subtracting from original **(M1)**
 0.85×35000 OR $35000 - 0.15 \times 35000$
 $= (\$)29750$ **A1**

Note: Accept $(\$)29800$.

[2 marks]

- (b) **EITHER**

$$29750 \times 0.89^9$$

(A1)

OR

$$N = 9$$

$$I\% = -11$$

$$PV = \mp 29750$$

(A1)

THEN

$$\text{value}(FV) = (\$)10423$$

A1

Note: For this **A1** the answer must be rounded to the nearest dollar.
 Accept $(\$)10441$ from using 3 sf answer from part (a).

[2 marks]

continued...

Question 2 continued

(c) **METHOD 1**

attempt to solve the inequality (or equation) $29750 \times 0.89^{n-1} < 3500$ OR table of values **(M1)**

19.3643... OR $(n = 19 \Rightarrow) 3651.80...$ OR $(n = 20 \Rightarrow) 3250.10...$ **(A1)**

Note: For candidates using (\$)29800, $n > 19.3787...$, $(n = 19 \Rightarrow) 3657.93...$,
 $(n = 20 \Rightarrow) 3255.56...$

$n = 20$

A1

[3 marks]

METHOD 2

use of the finance app with $I\% = -11$, $PV = \mp 29750$, $FV = \pm 3500$

OR $29750 \times 0.89^N < 3500$ (condone the use of n or x) **(M1)**

$(N =) 18.3643...$ **(A1)**

Note: For candidates using (\$)29800, $N = 18.3787...$

$n = 20$

A1

[3 marks]

Total [7 marks]

3. (a) attempt to use trigonometry to find the radius of the cone OR Oliver's distance from centre $(r+5)$ (M1)

$$\tan 58^\circ = \frac{18.2}{r+5} \quad \text{OR} \quad \frac{r+5}{\sin 32^\circ} = \frac{18.2}{\sin 58^\circ} \quad \text{OR} \quad (r+5) = 11.3726... \quad \text{(A1)}$$

$$r = 6.37262... \text{ (m)}$$

$$(r =) 6.37 \text{ (m)}$$

A1

[3 marks]

- (b) attempt to substitute $h = 20$ and their radius into the correct volume of cone formula (M1)

$$V = \frac{\pi(6.37262...)^2(20)}{3}$$

$$= 850.540...$$

$$= 851 \text{ (m}^3\text{)}$$

A1

Note: Accept 849.840... (850) obtained from using $r = 6.37$.

[2 marks]

Total [5 marks]

4. (a) recognition of $X > 13$ OR $Z > 1.5$ (could be seen in a diagram) **(M1)**

$$P(X > 13) = 0.0668072...$$

$$= 0.0668$$

A1

[2 marks]

- (b) **EITHER**

equating an appropriate correct normal CDF function to 0.1 or 0.9 **(M1)**

$$P(X > 10 + 2k) = 0.1 \text{ OR } P(Z < k) = 0.9 \text{ OR } P(X < 10 - 2k) = 0.1 \text{ OR } P(Z < -k) = 0.1$$

OR

recognising need to use inverse normal with 0.1 or 0.9 **(M1)**

THEN

$$1.28155...$$

$$k = 1.28$$

A1

Total [4 marks]

5. (a) recognition that velocity is zero (M1)

$$v = 2 \sin(0.5t) + 0.3t - 2 = 0$$

$$t = 1.68694\dots$$

$$t = 1.69$$

A1

[2 marks]

- (b) recognition that $v > 0$ (M1)

$$1.68694\dots < t < 6.11857\dots$$

$$1.69 < t < 6.12$$

A1

[2 marks]

- (c) attempt to substitute into the total displacement formula (condone missing or incorrect limits, and absence of dt) (M1)

$$\int_0^{10} (2 \sin(0.5t) + 0.3t - 2) dt \quad \text{OR} \quad \int_0^{10} v(t) dt$$

$$= -2.13464\dots$$

$$= -2.13 \text{ (m)}$$

A1

Note: Award (M1)A0 if -2.13 is followed by 2.13 .

[2 marks]

Total [6 marks]

6. (a) $r = 0.901017\dots$

$r = 0.901$

A2

[2 marks]

(b) Student 11 Test B: should not extrapolate

R1

[1 mark]

(c) (i) Student 12 Test A: should not use line of y on x to predict x from y (or equivalent)

R1

(ii) attempt to find the equation of the regression line of x on y

(M1)

$(x =) 0.987124\dots y - 3.21970\dots \quad ((x =) 0.987y - 3.22)$

A1

$(x =) 0.987124\dots(90) - 3.21970\dots \quad (= 85.6214\dots)$

A1

$= 86$ to nearest integer.

AG

Note: Condone notation for x and y switched if values are correct.

[4 marks]

Total [7 marks]

Section B

7. (a) METHOD 1

attempt to interchange x and y

M1

Note: This **M1** may be awarded at any stage in the working.

attempt to rearrange using definition of natural log or take the natural log of both sides

M1

$$\frac{2x}{3} = e^{y-2} \Rightarrow \ln\left(\frac{2x}{3}\right) = y-2 \quad \text{OR} \quad x = \frac{3}{2}e^{y-2} \Rightarrow \ln(x) = \ln\left(\frac{3}{2}\right) + y-2$$

A1

$$y = 2 + \ln\left(\frac{2x}{3}\right)$$

$$\text{so } f^{-1}(x) = 2 + \ln\left(\frac{2x}{3}\right)$$

AG

[3 marks]

METHOD 2

attempt to verify that $(f \circ f^{-1})(x) = x$

M1

$$(f \circ f^{-1})(x) = \frac{3}{2}e^{\ln\left(\frac{2x}{3}\right)+2-2} = \frac{3}{2}e^{\ln\left(\frac{2x}{3}\right)}$$

attempt to use definition of natural log

M1

$$(f \circ f^{-1})(x) = \frac{3}{2} \times \frac{2x}{3}$$

A1

$$(f \circ f^{-1})(x) = x$$

AG

[3 marks]

continued...

Question 7 continued

- (b) (0.264456..., 0.264456...) AND (2.51799..., 2.51799...) (A1)

Note: Award **A1** for 0.264456... and 2.51799... seen.

attempt to put their values in distance formula or use of the isosceles right-angled triangle (M1)

$$\sqrt{(2.51799... - 0.264456...)^2 + (2.51799... - 0.264456...)^2} \text{ OR}$$

$$\sqrt{2} \times (2.51799... - 0.264456...)$$

$$= 3.18689...$$

$$= 3.19$$

A1

[3 marks]

- (c) (i) $g(x) = -\frac{3}{2}e^{x-2} + 5$ OR $g(x) = -f(x) + 5$ A1A1

Note: Award **A1** for each correct term.

(ii) $0 \leq x \leq 4$

A1

[3 marks]

(d) $\frac{3}{2}e^{x-2} = -\frac{3}{2}e^{x-2} + 5$ OR $f(x) = -f(x) + 5$

attempt to collect together terms in e^{x-2} or $f(x)$ (M1)

$$3e^{x-2} = 5 \text{ OR } 2f(x) = 5$$

$$e^{x-2} = \frac{5}{3} \text{ OR } x = f^{-1}\left(\frac{5}{2}\right)$$

(A1)

$$x = 2 + \ln\left(\frac{5}{3}\right)$$

A1

$$\left(a = 2, b = \frac{5}{3}\right)$$

Note: Award **A1** for each correct term given in exact form.

[3 marks]

Total [12 marks]

8. (a) **EITHER**

attempt to find value of t for the first low tide OR the first high tide (M1)

$$11.2619... - 5.13801...$$

$$= 6.12396... \quad (A1)$$

OR

attempt to find half of the period (M1)

$$\frac{1}{2} \times \frac{2\pi}{0.513}$$

$$= 6.12396... \quad (A1)$$

THEN

$$m = (6.12396... - 6) \times 60 = 7.43773...$$

$$m = 7 \quad A1$$

[3 marks]

(b) attempt to solve $H(t) = 1$ (M1)

$$3.56919... \text{ OR } 6.70684... \text{ OR } 15.8171... \text{ OR } 18.9547...$$

$$(6.70684... - 3.56919...) = 3.13764...$$

$$= 3.14 \text{ (hours)} \quad A1$$

[2 marks]

(c) recognition that $H'(13)$ is required (M1)

$$= -0.650622...$$

$$= -0.651 \text{ (m/h)} \quad A1$$

[2 marks]

continued...

Question 8 continued

(d)

Note: In part (d), award the marks for a , b , c and d independent of each other.

METHOD 1

$$a = 1.17 \quad \text{A1}$$

$$d = 1.57 \quad \text{A1}$$

attempt to find time between low and high tide in hours (M1)

6 hours and 21 minutes = 6.35 hours

(period =) 12.7 (A1)

$$b = \frac{2\pi}{12.7} = 0.494739\dots$$

$$b = 0.495 \left(= \frac{60\pi}{381} \right) \quad \text{A1}$$

attempt to find mean of low and high tide times OR substitute values of a known point (M1)

$$c = \frac{1}{2} \left(2\frac{41}{60} + 9\frac{2}{60} \right) \text{ OR eg } 0.40 = 1.17 \sin(0.495(2.68333\dots - c)) + 1.57$$

$$c = 5.85833\dots$$

$$c = 5.86 \quad \text{A1}$$

Note: Award (M1)A1 for $c = 18.6$.
Award (M1)A0 for $c = -6.84$.

[7 marks]

continued...

Question 8 continued

METHOD 2

$$a = 1.17 \quad \text{A1}$$

$$d = 1.57 \quad \text{A1}$$

substituting at least one point into $h(t)$ (M1)

$$1.17 \sin \left(b \left(2 \frac{41}{60} - c \right) \right) + 1.57 = 0.4 \quad \text{OR} \quad 1.17 \sin \left(b \left(9 \frac{2}{60} - c \right) \right) + 1.57 = 2.74$$

$$b \left(2 \frac{41}{60} - c \right) = -\frac{\pi}{2} (= -1.57) \quad \text{AND} \quad b \left(9 \frac{2}{60} - c \right) = \frac{\pi}{2} (= 1.57) \quad \text{(A1)}$$

Note: accept any angles of the form $-\frac{\pi}{2} + 2\pi k$ and $\frac{\pi}{2} + 2\pi k$.

EITHER

use of graph or table to find their intersection (M1)

OR

attempt to solve their equations simultaneously (M1)

$$\frac{2 \frac{41}{60} - c}{9 \frac{2}{60} - c} = -1$$

THEN

$$c = 5.85833...$$

$$c = 5.86 \quad \text{A1}$$

$$b = 0.494739...$$

$$b = 0.495 \quad \text{A1}$$

[7 marks]

(e) attempt to find point of intersection of two graphs (M1)

$$T = 4.16292... \quad \text{OR} \quad T = 4.16417... \text{ (using 3 sf)}$$

$$T = 4.16 \quad \text{A1}$$

[2 marks]

Total [16 marks]

9. (a) (i) **METHOD 1**

attempt to use the sine rule to find $\hat{A}BO$ (M1)

$$\frac{25}{\sin 28^\circ} = \frac{50}{\sin \hat{A}BO}$$

$$(\hat{A}BO =) 69.8748\dots^\circ \text{ or } (\hat{A}BO =) 110.125\dots^\circ \quad \text{(A1)(A1)}$$

Note: Award **A1** for each value.

attempt to find at least one possible angle for $\hat{O}AB$ (M1)

$$(\hat{O}AB =) 180^\circ - 28^\circ - 69.8748\dots^\circ \text{ OR } (\hat{O}AB =) 180^\circ - 28^\circ - 110.125\dots^\circ$$

$$\hat{O}AB = 82.1251\dots^\circ, 41.8748\dots^\circ$$

$$\hat{O}AB = 82.1^\circ, 41.9^\circ \quad \text{A1}$$

METHOD 2

attempt to use the cosine rule to find OB (M1)

$$25^2 = 50^2 + OB^2 - 2(50)(OB)\cos 28^\circ$$

$$OB = 52.7491\dots \text{ or } 35.5455\dots \quad \text{(A1) (A1)}$$

attempt to use the sine rule to find $\hat{O}AB$ (M1)

$$\frac{25}{\sin 28^\circ} = \frac{OB}{\sin \hat{O}AB}$$

$$\hat{O}AB = 82.1251\dots^\circ, 41.8748\dots^\circ$$

$$\hat{O}AB = 82.1^\circ, 41.9^\circ \quad \text{A1}$$

continued...

Question 9 continued

- (ii) attempt to substitute two sides of triangle OAB and one of their angles into the area formula $\frac{1}{2}ab \sin C$ (M1)

$$\frac{1}{2}(OA)(AB) \sin 82.1251...^\circ \text{ OR } \frac{1}{2}(50)(25) \sin 41.8748...^\circ \text{ OR}$$

$$\frac{1}{2}(50)(52.7491...) \sin 28^\circ \text{ OR } \frac{1}{2}(50)(35.5455) \sin 28^\circ$$

$$\text{Area} = 619.106... \text{ OR } = 417.190...$$

$$= 619 \text{ (m}^2\text{)} \text{ OR } = 417 \text{ (m}^2\text{)}$$

A1A1

[8 marks]

- (b) attempt to use the cosine rule in triangle OCD (M1)

$$10^2 = x^2 + y^2 - 2xy \cos 28^\circ$$

A1

- attempt to use the area formula in triangle OCD (M1)

$$\frac{1}{2}xy \sin 28^\circ = 60$$

A1

Note: Award (M1)A1 for use of the area formula independently of the (M1)A1 for use of the cosine rule.

$$xy = \frac{120}{\sin 28^\circ}$$

$$100 = x^2 + y^2 - \frac{240 \cos 28^\circ}{\sin 28^\circ}$$

A1

$$x^2 + y^2 = 100 + \frac{240}{\tan 28^\circ}$$

AG

[5 marks]

continued...

Question 9 continued

(c) **EITHER**

attempt to eliminate y or x

(M1)

$$100 = x^2 + \left(\frac{120}{x \sin 28^\circ} \right)^2 - \frac{240}{\tan 28^\circ}$$

OR

attempt to find the intersection of the graph of their cosine rule equation and the graph of their area formula

(M1)

Note: Award **(M1)** only if their graphs are of functions with the same subject e.g. both " $y = \dots$ " or both " $y^2 = \dots$ ".

THEN

$$x = 13.1300\dots \text{ or } x = 19.4673\dots$$

$$x = 13.1 \text{ or } x = 19.5$$

A1A1

$$\text{OC} = 13.1(\text{m}) \text{ or } 19.5(\text{m})$$

[3 marks]

Total [16 marks]
