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Mathematics: analysis and approaches

Standard level

Paper 1

15 May 2025

Zone A afternoon | Zone B afternoon | Zone C afternoon

Candidate session number

1 hour 30 minutes

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Instructions to candidates

- Write your session number in the boxes above.
- Do not open this examination paper until instructed to do so.
- You are not permitted access to any calculator for this paper.
- Section A: answer all questions. Answers must be written within the answer boxes provided.
- Section B: answer all questions in the answer booklet provided. Fill in your session number on the front of the answer booklet, and attach it to this examination paper and your cover sheet using the tag provided.
- Unless otherwise stated in the question, all numerical answers should be given exactly or correct to three significant figures.
- A clean copy of the **mathematics: analysis and approaches SL formula booklet** is required for this paper.
- The maximum mark for this examination paper is **[80 marks]**.



Full marks are not necessarily awarded for a correct answer with no working. Answers must be supported by working and/or explanations. Where an answer is incorrect, some marks may be given for a correct method, provided this is shown by written working. You are therefore advised to show all working.

Section A

Answer **all** questions. Answers must be written within the answer boxes provided. Working may be continued below the lines, if necessary.

1. [Maximum mark: 5]

Write each of the following expressions in the form $\ln k$, where $k \in \mathbb{Z}^+$.

(a) $\ln 3 + \ln 4$ [1]

(b) $3 \ln 2$ [2]

(c) $-\ln \frac{1}{2}$ [2]

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2. [Maximum mark: 5]

Consider the function $f(x) = \frac{4x^3}{3} - 16x$, where $x \in \mathbb{R}$.

The graph of $y = f(x)$ has a local minimum point at (p, q) where $p > 0$.

Find the value of p and the value of q .

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3. [Maximum mark: 7]

Bob invests 1000 dinar in an account which pays a nominal annual interest rate of 4% compounded **quarterly**.

The amount of money in the account after one complete year can be written as $1000(1 + k)^4$ where $k \in \mathbb{Q}$.

(a) Write down the value of k . [1]

(b) Expand and simplify $(1 + x)^4$. [2]

(c) Hence or otherwise, find the amount of money in the account after one complete year, giving your answer correct to the nearest dinar. [4]

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4. [Maximum mark: 4]

Find the area completely enclosed by the curves $y = e^x$, $y = -e^x$, and the lines $x = -1$ and $x = 1$.

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5. [Maximum mark: 6]

Consider events A and B such that $P(A') = P(A \cup B) = \frac{3}{4}$ and $P(B|A) = \frac{2}{3}$.

(a) Find $P(A \cap B)$. [3]

(b) Show that events A and B are independent. [3]

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6. [Maximum mark: 8]

Consider a sequence of ten rectangular picture frames $F_1, F_2, \dots, F_9, F_{10}$.

Picture frame F_1 has width 4 cm and height 5 cm.

The width and height of picture frame F_n , are each increased by 50% to generate the width and height of the next picture frame F_{n+1} , for $n \in \mathbb{Z}^+$, $1 \leq n \leq 9$.

(a) (i) Show that the area of picture frame F_n is $20\left(\frac{9}{4}\right)^{n-1} \text{ cm}^2$.

(ii) Hence, find the mean area of the ten picture frames, giving your answer in the form $p\left(\left(\frac{9}{4}\right)^a - 1\right) \text{ cm}^2$, where $p \in \mathbb{Q}^+$, $a \in \mathbb{Z}^+$. [5]

(b) Find the median area of the ten picture frames, giving your answer in the form $q\left(\frac{9}{4}\right)^4 \text{ cm}^2$, where $q \in \mathbb{Q}^+$. [3]

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Section B

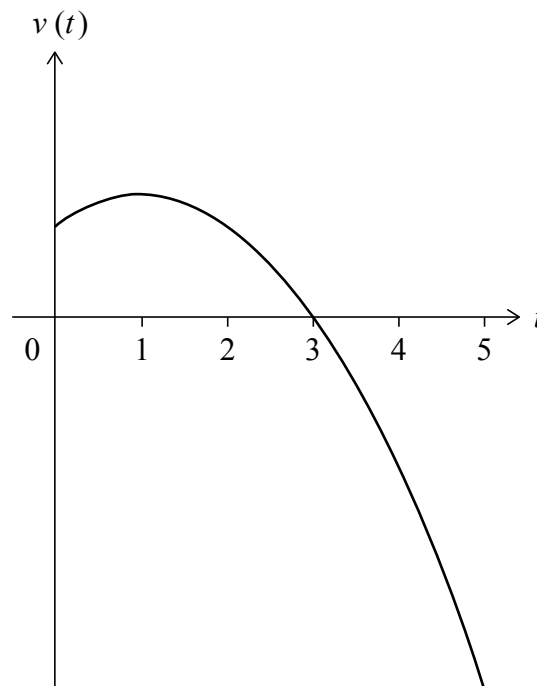
Answer **all** questions in the answer booklet provided. Please start each question on a new page.

7. [Maximum mark: 13]

An object moves in a straight line.

Its velocity $v \text{ m s}^{-1}$, at time t seconds, is given by $v(t) = 30 + 20t - 10t^2$ for $0 \leq t \leq 5$.

The graph of v is shown in the following diagram.



The graph of v has a local maximum point where $t = 1$ and intersects the t -axis at $t = 3$.

(a) Determine the object's

- (i) maximum velocity;
- (ii) maximum speed.

[4]

At $t = T$, the object changes direction.

(b) (i) Write down the value of T .

(ii) Find the distance travelled by the object in the first T seconds.

[5]

(c) Determine whether the object returns to its initial position during the time period $0 \leq t \leq 5$, justifying your answer.

[4]



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8. [Maximum mark: 15]

The function f is defined by $f(x) = 5(x + 1)(x + 3)$, where $x \in \mathbb{R}$.

- (a) Write $f(x)$ in the form $a(x - h)^2 + k$, where $a, h, k \in \mathbb{Z}$. [4]
- (b) Sketch the graph of $y = f(x)$, showing the values of any intercepts with the axes and the coordinates of the vertex. [4]
- (c) Solve the inequality $f(x) \leq 40$. [4]

The function g is defined by $g(x) = \ln x$, where $x \in \mathbb{R}$, $x > 0$.

- (d) (i) Write down an expression for $(f \circ g)(x)$.
- (ii) Solve the inequality $(f \circ g)(x) \leq 40$. [3]



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9. [Maximum mark: 17]

A solid cylinder has height h cm and base radius R cm.

The cylinder fits exactly inside a hollow sphere of radius r cm.

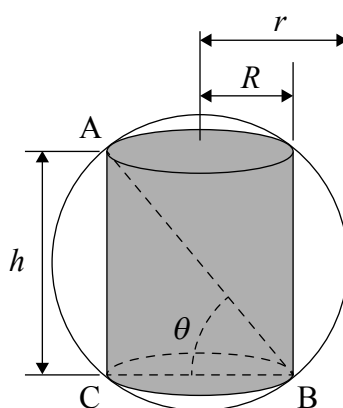
Points A , B and C are points where the surface of the cylinder touches the surface of the sphere.

The line segment $[AB]$ is a diameter of the sphere.

The line segment $[BC]$ is a diameter of the base of the cylinder and $\hat{ABC} = \theta$.

This information is shown on the following diagram.

diagram not to scale



(a) (i) By considering triangle ABC , show that $R = r \cos \theta$.

(ii) Find an expression for h in terms of r and θ . [4]

(b) Hence or otherwise, show that the total surface area, $S \text{ cm}^2$, of the cylinder is given by $S = 2\pi r^2 (1 + 2 \sin \theta \cos \theta - \sin^2 \theta)$. [4]

The external surface area of the sphere is $2S$.

(c) Show that $\tan \theta = 2$. [4]

The volume of the cylinder is $V \text{ cm}^3$.

(d) Find V , giving your answer in the form $p\pi r^3 \sqrt{5}$, where $p \in \mathbb{Q}^+$. [5]



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12EP11

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12EP12